

# Integral measurements of plural and multiple scattering of electrons with energies between 10 and 100 keV for $6 \leq Z \leq 83$ : I. Thin and intermediate-thickness targets

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## SUPPLEMENTAL MATERIAL POLYNOMIAL FITS

The coefficients of the polynomial

$$y(x) = \sum_{i=0}^n a_i x^i \quad (1)$$

that have been fitted to the charge fraction measured in the Faraday cup and aluminium ring, see paper for more details, are given in the following tables. The values for the two thin C targets are given in Table 1. The thin Al, Cu, Te, Au, and Bi<sub>2</sub>O<sub>3</sub> targets with C backing are considered in Tables 2, 3, 4, 5, and 6, respectively. Finally, the values for the intermediate self-supporting Al, Cu, and Au targets are reported in Tables 7, 8, and 9, respectively.

Table 1: Parameters fitted to the charge fraction in the Faraday cup and aluminium ring for the thin C target A.

| Coefficients | C target A             |                        | Target B               |                        |
|--------------|------------------------|------------------------|------------------------|------------------------|
|              | Faraday cup            | Ring                   | Faraday cup            | Ring                   |
| $a_0$        | +0.304                 | +0.307                 | +0.195                 | +0.388                 |
| $a_1$        | +0.074                 | −0.033                 | +0.089                 | −0.044                 |
| $a_2$        | $−3.60 \cdot 10^{-3}$  | $+1.59 \cdot 10^{-3}$  | $−4.43 \cdot 10^{-3}$  | $+2.22 \cdot 10^{-3}$  |
| $a_3$        | $+9.68 \cdot 10^{-5}$  | $−4.32 \cdot 10^{-5}$  | $+1.24 \cdot 10^{-4}$  | $−6.30 \cdot 10^{-5}$  |
| $a_4$        | $−1.53 \cdot 10^{-6}$  | $+6.93 \cdot 10^{-7}$  | $−2.07 \cdot 10^{-6}$  | $+1.05 \cdot 10^{-6}$  |
| $a_5$        | $+1.43 \cdot 10^{-8}$  | $−6.52 \cdot 10^{-9}$  | $+2.03 \cdot 10^{-8}$  | $−1.03 \cdot 10^{-8}$  |
| $a_6$        | $−7.22 \cdot 10^{-11}$ | $+3.32 \cdot 10^{-11}$ | $−1.08 \cdot 10^{-10}$ | $+5.48 \cdot 10^{-11}$ |
| $a_7$        | $+1.53 \cdot 10^{-13}$ | $−7.09 \cdot 10^{-14}$ | $−2.42 \cdot 10^{-13}$ | $−1.22 \cdot 10^{-13}$ |

Table 2: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the thin Al/C target.

| Coefficients | Al/C                   |                        |
|--------------|------------------------|------------------------|
|              | Faraday cup            | Ring                   |
| $a_0$        | −0.219                 | +0.435                 |
| $a_1$        | +0.103                 | −0.033                 |
| $a_2$        | $−3.87 \cdot 10^{-3}$  | $+1.16 \cdot 10^{-3}$  |
| $a_3$        | $+7.85 \cdot 10^{-5}$  | $−2.20 \cdot 10^{-5}$  |
| $a_4$        | $−8.89 \cdot 10^{-7}$  | $+2.36 \cdot 10^{-7}$  |
| $a_5$        | $+5.29 \cdot 10^{-9}$  | $−1.34 \cdot 10^{-9}$  |
| $a_6$        | $−1.29 \cdot 10^{-11}$ | $+3.15 \cdot 10^{-12}$ |

Table 3: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the thin Cu/C target.

| Cu/C         |                        |                        |
|--------------|------------------------|------------------------|
| Coefficients | Faraday cup            | Ring                   |
| $a_0$        | -0.297                 | -0.447                 |
| $a_1$        | +0.068                 | +0.153                 |
| $a_2$        | $-1.67 \cdot 10^{-3}$  | $-1.40 \cdot 10^{-2}$  |
| $a_3$        | $+2.17 \cdot 10^{-5}$  | $+6.65 \cdot 10^{-4}$  |
| $a_4$        | $-1.44 \cdot 10^{-7}$  | $-1.92 \cdot 10^{-5}$  |
| $a_5$        | $+3.85 \cdot 10^{-10}$ | $+3.54 \cdot 10^{-7}$  |
| $a_6$        | -                      | $-4.20 \cdot 10^{-9}$  |
| $a_7$        | -                      | $+3.10 \cdot 10^{-11}$ |
| $a_8$        | -                      | $-1.29 \cdot 10^{-13}$ |
| $a_9$        | -                      | $+2.34 \cdot 10^{-16}$ |

Table 4: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the thin Te/C target.

| Te/C         |                       |                        |
|--------------|-----------------------|------------------------|
| Coefficients | Faraday cup           | Ring                   |
| $a_0$        | -0.263                | -0.081                 |
| $a_1$        | +0.057                | +0.053                 |
| $a_2$        | $-1.19 \cdot 10^{-3}$ | $-3.56 \cdot 10^{-3}$  |
| $a_3$        | $+1.32 \cdot 10^{-5}$ | $+1.11 \cdot 10^{-4}$  |
| $a_4$        | $-7.53 \cdot 10^{-8}$ | $-1.95 \cdot 10^{-6}$  |
| $a_5$        | $1.73 \cdot 10^{-10}$ | $+1.95 \cdot 10^{-8}$  |
| $a_6$        | -                     | $-1.05 \cdot 10^{-10}$ |
| $a_7$        | -                     | $+2.36 \cdot 10^{-13}$ |

Table 5: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the thin Au/C target.

| Au/C         |                        |                        |
|--------------|------------------------|------------------------|
| Coefficients | Faraday cup            | Ring                   |
| $a_0$        | +0.230                 | +0.210                 |
| $a_1$        | +0.062                 | -0.014                 |
| $a_2$        | $-2.36 \cdot 10^{-3}$  | $+4.47 \cdot 10^{-4}$  |
| $a_3$        | $+4.94 \cdot 10^{-5}$  | $-8.37 \cdot 10^{-6}$  |
| $a_4$        | $-5.78 \cdot 10^{-7}$  | $+9.08 \cdot 10^{-8}$  |
| $a_5$        | $+3.55 \cdot 10^{-9}$  | $-5.30 \cdot 10^{-10}$ |
| $a_6$        | $-8.91 \cdot 10^{-12}$ | $+1.29 \cdot 10^{-12}$ |

Table 6: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the thin Bi<sub>2</sub>O<sub>3</sub>/C target.

| Bi <sub>2</sub> O <sub>3</sub> /C |                        |                        |
|-----------------------------------|------------------------|------------------------|
| Coefficients                      | Faraday cup            | Ring                   |
| $a_0$                             | -0.322                 | +0.399                 |
| $a_1$                             | +0.101                 | -0.024                 |
| $a_2$                             | $-3.60 \cdot 10^{-3}$  | $+6.22 \cdot 10^{-4}$  |
| $a_3$                             | $+7.06 \cdot 10^{-5}$  | $-8.51 \cdot 10^{-6}$  |
| $a_4$                             | $-7.79 \cdot 10^{-7}$  | $+5.86 \cdot 10^{-8}$  |
| $a_5$                             | $+4.54 \cdot 10^{-9}$  | $-1.60 \cdot 10^{-10}$ |
| $a_6$                             | $-1.09 \cdot 10^{-11}$ | -                      |

Table 7: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the intermediate Al target.

| Al           |                        |                        |
|--------------|------------------------|------------------------|
| Coefficients | Faraday cup            | Ring                   |
| $a_0$        | +0.080                 | -0.186                 |
| $a_1$        | -0.014                 | +0.035                 |
| $a_2$        | $+1.49 \cdot 10^{-3}$  | $-7.81 \cdot 10^{-4}$  |
| $a_3$        | $-3.02 \cdot 10^{-5}$  | $-1.96 \cdot 10^{-6}$  |
| $a_4$        | $+2.56 \cdot 10^{-7}$  | $+2.31 \cdot 10^{-7}$  |
| $a_5$        | $-8.00 \cdot 10^{-10}$ | $-2.52 \cdot 10^{-9}$  |
| $a_6$        | -                      | $+8.66 \cdot 10^{-12}$ |

Table 8: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the intermediate Cu target.

| Cu           |                        |                        |
|--------------|------------------------|------------------------|
| Coefficients | Faraday cup            | Ring                   |
| $a_0$        | $-3.72 \cdot 10^{-3}$  | -0.032                 |
| $a_1$        | $-3.28 \cdot 10^{-3}$  | $-1.30 \cdot 10^{-4}$  |
| $a_2$        | $+5.78 \cdot 10^{-4}$  | $+5.05 \cdot 10^{-4}$  |
| $a_3$        | $-2.24 \cdot 10^{-5}$  | $-1.37 \cdot 10^{-5}$  |
| $a_4$        | $+4.29 \cdot 10^{-7}$  | $+1.42 \cdot 10^{-7}$  |
| $a_5$        | $-3.80 \cdot 10^{-9}$  | $-5.27 \cdot 10^{-10}$ |
| $a_6$        | $+1.25 \cdot 10^{-11}$ | -                      |

Table 9: Parameters fitted for the charge fraction in the Faraday cup and aluminium ring for the intermediate Au target.

| Au           |                       |                       |
|--------------|-----------------------|-----------------------|
| Coefficients | Faraday cup           | Ring                  |
| $a_0$        | +0.033                | -0.062                |
| $a_1$        | $-2.21 \cdot 10^{-3}$ | +0.016                |
| $a_2$        | $+3.91 \cdot 10^{-4}$ | $-3.07 \cdot 10^{-4}$ |
| $a_3$        | $-5.08 \cdot 10^{-6}$ | $+2.19 \cdot 10^{-6}$ |
| $a_4$        | $+2.05 \cdot 10^{-8}$ | $-5.45 \cdot 10^{-9}$ |